# A mathematical model for the spatiotemporal epidemic spreading of COVID19

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An outbreak of a novel coronavirus, named SARS-CoV-2, that provokes the COVID-19 disease, was first reported in Hubei, mainland China on 31 December 2019. As of 20 March 2020, cases have been reported in 166 countries/regions, including cases of human-to-human transmission around the world. The proportions of this epidemics is probably one of the largest challenges faced by our interconnected modern societies. According to the current epidemiological reports, the large basic reproduction number,  $R_0 \sim 2.3$ , number of secondary cases produced by an infected individual in a population of susceptible individuals, as well as an asymptomatic period (up to 14 days) in which infectious individuals are undetectable without further analysis, pave the way for a major crisis of the national health capacity systems. Recent scientific reports have pointed out that the detected cases of COVID19 at young ages is strikingly short and that lethality is concentrated at large ages. Here we adapt a Microscopic Markov Chain Approach (MMCA) metapopulation mobility model to capture the spread of COVID-19. We propose a model that stratifies the population by ages, and account for the different incidences of the disease at each strata. The model is used to predict the incidence of the epidemics in a spatial population through time, permitting investigation of control measures. The model is applied to the current epidemic in Spain, using the estimates of the epidemiological parameters and the mobility and demographic census data of the national institute of statistics (INE). The results indicate that the peak of incidence will happen in the first half of April 2020 in absence of mobility restrictions. These results can be refined with improved estimates of epidemiological parameters, and can be adapted to precise mobility restrictions at the level of municipalities, The current estimates largely compromises the Spanish health capacity system, in particular that for intensive care units, from the end of March. However, the model allows for the scrutiny of containment measures that can be used for health authorities to forecast with accuracy their impact in prevalence of COVID-19. Here we show by testing different epidemic containment scenarios that we urge to enforce total lockdown to avoid a massive collapse of the Spanish national health system.

#### I. INTRODUCTION

As of 20 March 2020 the outbreak of the novel coronavirus, SARS-CoV-2, has infected more than 270.000 persons worldwide with COVID-19, killing more than 11.300. Epidemiological analysis of the outbreak have been used to estimate epidemiologically relevant parameters [1–10], and available mathematical models have been used to track and anticipate the spread of the epidemics [11–17]. Nevertheless, the particularities of the current epidemics calls for a rethinking of conventional models towards tailored ones. Here, we propose mathematical model particularly designed to capture the main ingredients characterising the propagation of SARS-CoV-2 and the clinical characteristics reported for the cases of COVID-19. To this aim, we rely on previous metapopulation models by the authors [18–21] including the spatial demographical distribution and recurrent mobility patterns, and develop a more refined epidemic model that incorporates the stratification of population by age in order to consider the different epidemiological and clinical features associated to each group age that have been reported so far. The mathematical formulation of these models rely on the Microscopic Markov Chain Approach formulation for epidemic spreading in complex networks [22–27].

The epidemic model we propose takes into account several specific characteristics of the dynamics of COVID-19, such as the important effect of asymptomatic (or with mild symptoms) infectious individuals, which may explain the large incidence of the epidemics. We also consider the fraction of individuals which require hospitalization to ICU, since their saturation constitutes one of the major political and health problems of COVID-19 outbreak. The result is a model with seven epidemiological compartments for each of the patches composing the metapopulation. Additionally, we split the former epidemiological partition into three age groups: young, adults, and elderly people. This partition allows us to capture in a stylised way the main epidemiological, clinical and behavioural differences between the groups. On one hand, SARS-CoV-2 importation and exportation events

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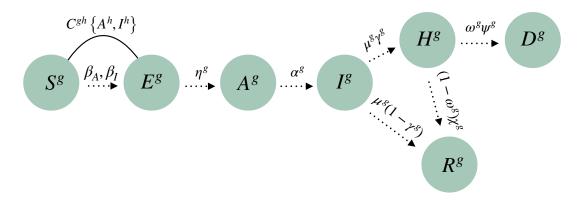


FIG. 1. Compartemental epidemic model proposed in this study. The acronyms are susceptible  $(S^g)$ , exposed  $(E^g)$ , asymptomatic infectious  $(A^g)$ , infected  $(I^g)$ , hospitalized to ICU  $(H^g)$ , dead  $(D^g)$ , and recovered  $(R^g)$ , where g denotes for all cases the age stratum.

between patches are mostly due to the mobility of active population. On the other hand, the medical evolution of COVID-19 displays strong differences across age groups [13, 28, 29]. In this regard, infections in the young group lead to mild symptoms [30] that, without test, are often confused with those of a common cold, whereas for old individuals the infection evolves towards more severe symptoms and usually requires hospitalization.

The model incorporates the possibility of designing and evaluating the impact of contention policies to stop the propagation of SARS-CoV-2. In particular, we focus on those policies relying on global or targeted quarantine measures. They allow the selection of the optimum degree of mobility to avoid the health system crisis. Taking advantage of this possibility, we explore several epidemic scenarios characterized by different contention measures promoted on March 20, and evaluate their impact on the decrease of the epidemic prevalence and the saturation of the Spanish health system.

In a nutshell, the proposed model takes into account in an stylized way three main ingredients taking place in SARS-CoV-2 transmission: (i) the silent transmission of the pathogen through the young portion of the population, (ii) the large potential for the spatial dissemination of the pathogen provided by the mobility of mature individuals, and (iii) the severe symptoms caused of COVID-19 in elderly that yields to a dramatic increase of medical and hospital demands. Thus, the model can be viewed as three coevolving spreading processes with different spatio-temporal scales.

## II. EPIDEMIC SPREADING MODEL

We propose a tailored model for the epidemic spread of COVID-19. We use a previous framework for the study of epidemics in structured metapopulations, with heterogeneous agents, subjected to recurrent mobility patterns [18–20, 31]. To understand the geographical diffusion of the disease, as a result of human-human interactions in small geographical patches, one has to combine the contagion process with the long-range disease propagation due to human mobility across different spatial scales. For the case of epidemic modeling, the metapopulation scenario is as follows. A population is distributed in a set of patches, being the size (number of individuals) of each patch in principle different. The individuals within each patch are well-mixed, *i.e.*, pathogens can be transmitted from an infected host to any of the healthy agents placed in the same patch with the same probability. The second aspect of our metapopulation model concerns the mobility of agents. Each host is allowed to change its current location and occupy another patch, thus fostering the spread of pathogens at the system level. Mobility of agents between different patches is usually represented in terms of a network where nodes are locations while a link between two patches represents the possibility of moving between them.

We introduce a set of modifications to the standard metapopulation model to account for the different states relevant for the description of COVID-19, and also to substitute the well-mixing with a more realistic set of contacts. Another key point is the introduction of a differentiation of the course of the epidemics that depends on the demographic ages of the population. This differentiation is very relevant in light of the observation of a scarcely set of infected individuals at ages (< 25), and also because of the severe situations reported for people at older ages (> 65). Our model is composed of the following epidemiological compartments: susceptible (S), exposed (E), asymptomatic infectious (A), infected (I), hospitalized to ICU (H), dead (D), and recovered (R). Additionally, we divide the individuals in  $N_G$  age strata, and suppose the geographical area is divided in N regions or patches. Although we present the model in general form, its application to COVID-19 only makes use of the three age groups mentioned above ( $N_G$  = 3): young people (Y), with age up to 25; adults (M), with age between 26 and 65; and elderly people (O), with age larger than 65. See Figure 1 for an sketch of the compartmental epidemic model proposed.

We characterize the evolution of the fraction of agents in state  $m \in \{S, E, A, I, H, D, R\}$  and for each age stratum  $g \in \{1, \dots, N_G\}$ , associated with each patch  $i \in \{1, \dots, N\}$ , denoted in the following as  $\rho_i^{m,g}(t)$ . The temporal evolution of these

quantities is given by:

$$\rho_i^{S,g}(t+1) = \rho_i^{S,g}(t)(1 - \Pi_i^g(t)), \tag{1}$$

$$\rho_i^{E,g}(t+1) = \rho_i^{S,g}(t)\Pi_i^g(t) + (1-\eta^g)\rho_i^{E,g}(t), \tag{2}$$

$$\rho_i^{A,g}(t+1) = \eta^g \rho_i^{E,g}(t) + (1 - \alpha^g) \rho_i^{A,g}(t), \tag{3}$$

$$\rho_i^{I,g}(t+1) = \alpha^g \rho_i^{A,g}(t) + (1-\mu^g)\rho_i^{I,g}(t), \qquad (4)$$

$$\rho_i^{H,g}(t+1) = \mu^g \gamma^g \rho_i^{I,g}(t) + \omega^g (1 - \psi^g) \rho_i^{H,g}(t) + (1 - \omega^g) (1 - \chi^g) \rho_i^{H,g}(t) , \tag{5}$$

$$\rho_i^{D,g}(t+1) = \omega^g \psi^g \rho_i^{H,g}(t) + \rho_i^{D,g}(t),$$
(6)

$$\rho_i^{R,g}(t+1) = \mu^g(1-\gamma^g)\rho_i^{I,g}(t) + (1-\omega^g)\chi^g\rho_i^{H,g}(t) + \rho_i^{R,g}(t).$$
(7)

These equations correspond to a discrete-time dynamics, in which each time-step represents a day. They are built upon previous work on Microscopic Markov-Chain Approach (MMCA) modelization of epidemic spreading dynamics [22], but which has also been applied to other types of processes, *e.g.*, information spreading and traffic congestion [24, 25, 32].

The rationale of the model is the following. Susceptible individuals get infected by contacts with asymptomatic and infected agents, with a probability  $\Pi_i^g$ , becoming exposed. Exposed individuals turn into asymptomatic at a certain rate  $\eta^g$ , which in turn become infected at a rate  $\alpha^g$ . Once infected, two paths emerge, which are reached at an escape rate  $\mu^g$ . The first option is requiring hospitalization in an ICU, with a certain probability  $\gamma^g$ ; otherwise, the individuals become recovered. While being at ICU, individuals have a death probability  $\omega^g$ , which is reached at a rate  $\psi^g$ . Finally, ICUs discharge at a rate  $\chi^g$ , leading to the recovered compartment. See Table I for a summary of the parameters of the model, and their values to simulate the spreading of COVID-19 in Spain, which will be discussed in Subsec. IV A.

The value of  $\Pi_i^g(t)$  encodes the probability that a susceptible agent belonging to age group g and patch i contracts the disease. Under the model assumptions, this probability is given by:

$$\Pi_i^g(t) = (1 - p^g)P_i^g(t) + p^g \sum_{j=1}^N R_{ij}^g P_j^g(t),$$
(8)

where  $p^g$  denotes the degree of mobility of individuals within age group g, and  $P_i^g(t)$  denotes the probability that those agents get infected by the pathogen inside patch i. This way, the first term in the r.h.s. of Eq. (8) denotes the probability of contracting the disease inside the residence patch, whereas the second term contains those contagions taking place in any of the neighboring areas. Furthermore, we assume that the number of contacts increases with the density of each area according to a monotonously increasing function f. Finally, we introduce an age-specific contact matrix, C, whose elements  $C^{gh}$  define the fraction of contacts that individuals of age group g perform with individuals belonging to age group g. With the above definitions, g reads

$$P_{i}^{g}(t) = 1 - \prod_{h=1}^{N_{G}} \prod_{j=1}^{N} (1 - \beta_{A})^{z^{g} \langle k^{g} \rangle} f^{\left(\frac{n_{i}^{\text{eff}}}{s_{i}}\right)} C^{gh} \frac{n_{j\to i}^{A,h}(t)}{(n_{i}^{h})^{\text{eff}}} (1 - \beta_{I})^{z^{g} \langle k^{g} \rangle} f^{\left(\frac{n_{i}^{\text{eff}}}{s_{i}}\right)} C^{gh} \frac{n_{j\to i}^{I,h}(t)}{(n_{i}^{h})^{\text{eff}}} . \tag{9}$$

The exponents represent the number of contacts made by an agent of age group g in patch i with infectious individuals — compartments A and I, respectively — of age group h residing at patch j. Accordingly, the double product expresses the probability for an individual belonging to age group g not being infected while staying in patch i.

The term  $z^g \langle k^g \rangle f(n_i^{\text{eff}}/s_i)$  in Eq. (9) represents the overall number of contacts (infectious or non infectious), which increases with the density of patch i following function f, and also accounts for the normalization factor  $z^g$ , which is calculated as:

$$z^g = \frac{N^g}{\sum_{i=1}^N f\left(\frac{n_i^{\text{eff}}}{s_i}\right) (n_i^g)^{\text{eff}}},\tag{10}$$

where the effective population at patch i is given by

$$n_i^{\text{eff}} = \sum_{g=1}^{N_G} (n_i^g)^{\text{eff}},$$
 (11)

which is distributed in age groups of size

$$(n_i^g)^{\text{eff}} = \sum_{i} \left[ (1 - p^g) \delta_{ij} + p^g R_{ji}^g \right] n_j^g.$$
 (12)

The function f(x) governing the influence of population density has been selected, following [33], as:

$$f(x) = 1 + (1 - e^{-\xi x}). (13)$$

The last term of the exponents in Eq. (9) contains the probability that these contacts are contagious, which is proportional to  $n_{j\to i}^{m,h}$ , the expected number of individuals of age group h in the given infectious state m (either A or I) which have moved from region j to region i:

$$n_{j\to i}^{m,h}(t) = n_j^h \rho_j^{m,h}(t) \left[ (1-p^h)\delta_{ij} + p^h R_{ji}^h \right], \quad m \in \{A, I\}.$$
 (14)

The discrete time nature of this model allows for an easy computation of the time evolution of all the relevant variables, providing information at the regional level. See Sec. IV B for the details of its application to the COVID-19 outbreak in Spain. Additionally, the model is amenable for analytical inspection, which has allowed us to find the epidemic threshold, see Appendix A.

#### III. PREDICTION OF INCIDENCE UNDER MOBILITY RESTRICTIONS

Here we assess the performance of different containment measures to reduce the impact of COVID-19 using the mathematical model. To incorporate containment policies in our formalism, we assume that a given fraction of the population  $\kappa_0$  is isolated at home. In this sense, let us remark that parameter  $\kappa_0$  allows us to change the level of resolution while studying the propagation of COVID-19. Namely, with  $\kappa_0=0$  we recover the well-mixing assumption within the same municipality described in previous sections —since active population movements promote the interaction between members from different households— whereas  $\kappa_0=1$  isolates the households from each other, thus constraining the transmission dynamics at the level of household rather than municipality. From the former assumptions, we compute the average number of contacts of agents belonging to each group g as

$$\langle k_c^g \rangle = (1 - \kappa_0) \langle k^g \rangle + \kappa_0(\sigma - 1), \tag{15}$$

where the second term in the r.h.s. encodes those contacts occurring within the household, whose size (number of individuals) is assumed to be  $\sigma$  in average.

In this scenario, a relevant indicator to quantify the efficiency of the policy is the probability of one individual living in a household, inside a given municipality i, without any infected individual. Assuming that containment is implemented at time  $t_c$ , this quantity, denoted in the following as  $CH_i(t_c)$ , is given by

$$CH_{i}(t_{c}) = \left(\frac{\sum_{g=1}^{N_{G}} \left(\rho_{i}^{S,g}(t_{c}) + \rho_{i}^{R,g}(t_{c})\right) n_{i}^{g}}{\sum_{g=1}^{N_{G}} n_{i}^{g}}\right)^{\sigma},$$
(16)

and Eq. (15) becomes time-dependent:

$$\langle k^g \rangle (t) = (1 - \kappa_0 \Theta(t - t_c)) \langle k^g \rangle + \kappa_0 \Theta(t - t_c) (\sigma - 1), \tag{17}$$

where  $\Theta(x)$  is the Heaviside function, which is 1 if  $x \ge 0$  and 0 otherwise. Accordingly, the mobility parameters  $p^g$  change as

$$p^{g}(t) = (1 - \kappa_0 \Theta(t - t_c)) p^{g}, \tag{18}$$

which make  $(n_i^g)^{\text{eff}}$  and  $z^g$  also dependent on time, see Eqs. (10)–(12).

This containment strategy is introduced in the dynamical Eqs. (1)–(6) by modifying Eqs. (1) and (2) for the time after  $t_c$ :

$$\rho_i^{S,g}(t+1) = \rho_i^{S,g}(t)(1 - \delta_{t,t_c}\kappa_0 CH_i(t_c))(1 - \Pi_i^g(t)), \qquad (19)$$

$$\rho_i^{E,g}(t+1) = \rho_i^{S,g}(t)(1 - \delta_{t,t_c}\kappa_0 C H_i(t_c))\Pi_i^g(t) + (1 - \eta^g)\rho_i^{E,g}(t), \qquad (20)$$

$$\rho_i^{CH,g}(t) = \rho_i^{S,g}(t_c)\kappa_0 CH_i(t_c)\Theta(t - t_c), \qquad (21)$$

where we have added a new compartment CH to hold the individuals under household isolation after applying containment  $\kappa_0$ , and  $\delta_{a,b}$  is the Kronecker function, which is 1 if a=b and 0 otherwise. Containment also affects the average number of contacts, thus we must also update Eq. (9):

$$P_{i}^{g}(t) = 1 - \prod_{h=1}^{N_{G}} \prod_{i=1}^{N} (1 - \beta_{A})^{z^{g}(t)\langle k^{g}\rangle(t)f\left(\frac{n_{i}^{\text{eff}}(t)}{s_{i}}\right)C^{gh} \frac{n_{j\to i}^{A,h}(t)}{(n_{i}^{h})^{\text{eff}}(t)}} (1 - \beta_{I})^{z^{g}(t)\langle k^{g}\rangle(t)f\left(\frac{n_{i}^{\text{eff}}(t)}{s_{i}}\right)C^{gh} \frac{n_{j\to i}^{I,h}(t)}{(n_{i}^{h})^{\text{eff}}(t)}}.$$
 (22)

#### IV. RESULTS

### A. Parameters for the modelization of the spreading of COVID-19

In this subsection, we detail our parameters choice to study the current epidemic outbreak in Spain. Regarding epidemiological parameters, the incubation period has been reported to be  $\eta^{-1} + \alpha^{-1} = 5.2$  days [2] in average which, in our formalism, must be distributed into the exposed and asymptomatic compartments. In principle, if one does not expect asymptomatic transmissions, most of this time should be spent inside the exposed compartment, thus being the asymptomatic infectious compartment totally irrelevant for disease spreading. However, along the line of several recent works [34–36] we have found that the unfolding of COVID-19 cannot be explained without accounting for infections from individuals not developing any symptoms previously. In particular, our best fit to reproduce the evolution of the real cases reported so far in Spain yields  $\alpha^{-1}=2.86$  days as asymptomatic infectious period. In turn, the infection period is established as  $\mu^{-1}=3.2$  days [1, 12], except for the young strata, for which we have reduced it to 1 day, assigning the remaining 2.2 days as asymptomatic; this is due to the reported mild symptoms in young individuals, which may become inadvertent [30]. We fix the fatality rate  $\omega=42\%$  of ICU patients by studying historical records of dead individuals as a function of those requiring intensive care. In turn, we estimate the period from ICU admission to death as  $\psi^{-1}=7$  days [37] and the stay in ICU for those overcoming the disease as  $\chi^{-1}=10$  days [38].

Regarding the population structure in Spain, we have obtained the population distribution, population pyramid, daily population flows and average household size at the municipality level from Instituto Nacional de Estadística [39] whereas the age-specific contact matrices have been extracted from [40].

#### B. Prediction of the evolution of COVID-19 in Spain

Equations (1)–(7) enable to monitor the spatio-temporal propagation of COVID-19 across Spain. To check the validity of our formalism, we aggregate the number of cases predicted for each municipality at the level of autonomous regions (comunidades autónomas), which is a first-level political and administrative division, and compare them with the number of cases daily reported by the Spanish Health Ministry. In this sense, we compute the number of cases predicted for each municipality i at each time step t as:

$$Cases_{i}(t) = \sum_{q=1}^{N_{G}} \left( \rho_{i}^{R,g}(t) + \rho_{i}^{H,g}(t) + \rho_{i}^{D,g}(t) \right) n_{i}^{g}$$
(23)

As our model is designed to predict the emergence of autochthonous cases triggered by local contagions and commuting patterns, those imported infected individuals corresponding to the first reported cases in Spain are initially plugged into our model as asymptomatic infectious agents. In addition, small infectious seeds should be also placed in those areas where anomalous outbreaks have occurred due to singular events such as one funeral in Vitoria leading to more than 60 contagions. Overall, the total number of infectious seeds is 47 individuals which represents 0.2 % of the number of cases reported by March 20, 2020.

Figure 2 shows that our model is able to accurately predict not only the overall evolution of the total number of cases at the national scale but also their spatial distribution across the different autonomous regions. Moreover, the most typical trend observed so far is an exponential growth of the number of cases, thus clearly suggesting that the disease is spreading freely in most of the territories. Note, however, that there are some exceptions such as La Rioja or País Vasco in which some strong policies targeting the most affected areas were previously promoted to slow down COVID-19 propagation.

To assess the impact of containment policies, we now theoretically study the effects of tuning the isolation rate  $\kappa_0$  controlling the fraction of population staying at home. Figure 3 shows the temporal evolution of the individuals requiring intensive care units while applying the isolation policy by March 20, 2020. Interestingly, it becomes clear that there are two different regimes. For small  $\kappa_0$  values, the observed behavior corresponds to the flattening of the epidemic curve while promoting social distancing. This way, increasing  $\kappa_0$  leads to longer epidemic periods with much less impact within society in terms of hospitalized agents. In contrast, for large enough  $\kappa_0$  values, the effective isolation of households allows for reducing at the same time the epidemic size and the duration of the epidemic wave. This is mainly caused by the depletion [41] of susceptible individuals which prevents the infectious individuals from sustaining the outbreak by infecting healthy peers.

Finally, we address the important health problem arising from the saturation of ICU beds. For this purpose, we study the evolution of individuals requiring intensive care units by fixing  $\kappa_0=0.80$  from March 20, 2020. To quantify the overload of ICU capacity, in Figure 4 we compare the predictions yielded by our equations with the total number of beds within each autonomous region which we estimate as the 3% of the total number of hospital beds. There we find that the saturation of hospitals across Spain is not uniform but strongly depends on both the current extension of the outbreak and the available resources in each autonomous region.

Symbol	Description

$\beta_A$	Infectivity of asymptomatic	0.06
$eta_I$	Infectivity of infected	0.06
$\langle k^g \rangle$	Average number of contacts	(11.8, 13.3, 6.6)
$\eta^g$	Latent rate	$\frac{1}{2.34}$
$lpha^g$	Asymptomatic infectious rate	$\left(\frac{1}{5.06}, \frac{1}{2.86}, \frac{1}{2.86}\right)$
$\mu^g$	Escape rate	$\left(\frac{1}{1.0}, \frac{1}{3.2}, \frac{1}{3.2}\right)$
$\gamma^g$	Fraction of cases requiring ICU	(0.002, 0.05, 0.36)
$\omega^g$	Fatality rate of ICU patients	0.42
$\psi^g$	Death rate	$\frac{1}{7.0}$
$\chi^g$	ICU discharge rate	$\frac{1}{10.0}$
$n_i^g$	Regional population	Data provided by INE
$R_{ij}^g$	Mobility matrix	Data provided by INE
$C^{gh}$	Contacts-by-age matrix	$\begin{pmatrix} 0.5980 & 0.3849 & 0.0171 \\ 0.2440 & 0.7210 & 0.0350 \\ 0.1919 & 0.5705 & 0.2376 \end{pmatrix}$
ξ	Density factor	0.01
$p^g$	Mobility factor	(0.0, 1.0, 0.0)
$\sigma$	Average household size	2.5
$\kappa_0$	Confinement factor	Adjustable for containment

TABLE I. Parameters of the model and their estimations for COVID-19. See section IV.a for a detailed explanation.

# V. DISCUSSION

We have presented a mathematical model based on a Microscopic Markov Chain Approach (MMCA) for the spatio-temporal spreading of COVID-19. The model captures human behavior features such as: the urban demography, age strata, age-structured contact patterns, and daily recurrent mobility flows. Importantly, the epidemiological and human characteristics present in this model provides with the possibility of a rapid and reliable evaluation of different containment policies.

We have applied the results to the validation and projection of the propagation of COVID-19 in Spain. Our results reveal that, at the current stage of the epidemics, the application of stricter containment measures of social distance are urgent to avoid the collapse of the health system. Moreover, we are close to an scenario in which the complete lockdown appears as the only possible measure to avoid the former situation. Other scenarios can be prescribed and analyzed after lockdown, as for example pulsating open-closing strategies or targeted herd immunity.

### Appendix A: Calculation of epidemic threshold

The model is amenable for analytical calculations. We calculate the epidemic threshold using the next generation matrix approach [42]. Accordingly, we need to analyze the stability of the disease free equilibrium. We do so by making a first order expansion of the above equations for small values  $\epsilon$  of the non-susceptible states m:  $\epsilon \sim \rho_i^m \ll \rho_j^S \ \forall i,j$  and  $\rho_i^m \ll 1 \ \forall i$ , where  $m \in \{E,A,I,H,D,R\}$ . The expansion allows us to transform our discrete time Markov Chain into a continuous time differential equation. We start by expanding the infection probabilities  $P_i^g$ :

$$P_{i}^{g} = \sum_{h=1}^{N_{G}} \sum_{j=1}^{N} z^{g} \langle k^{g} \rangle f_{i} C^{gh} \frac{n_{j}^{h} \left[ (1-p^{h})\delta_{ij} + p^{h} R_{ji}^{h} \right]}{(n_{i}^{h})^{\text{eff}}} \left( b^{A} \rho_{j}^{A,h} + b^{I} \rho_{j}^{I,h} \right) + O(\epsilon^{2}), \tag{A1}$$

where we have defined

$$b^{m} = \ln\left[\left(1 - \beta_{m}\right)^{-1}\right], \ m \in \{A, I\}$$
 (A2)

and

$$f_i = f\left(\frac{n_i^{\text{eff}}}{s_i}\right). \tag{A3}$$

We then insert the above expression into  $\Pi_i^g$ , leading to:

$$\Pi_{i}^{g} = \sum_{h=1}^{N_{G}} \sum_{i=1}^{N} \left( (M_{1})_{ij}^{gh} + (M_{2})_{ij}^{gh} + (M_{3})_{ij}^{gh} + (M_{4})_{ij}^{gh} \right) \left( b^{A} \rho_{j}^{A,h} + b^{I} \rho_{j}^{I,h} \right) + O(\epsilon^{2}), \tag{A4}$$

where the above tensors  $M_{\ell}$  for  $\ell \in \{1, \dots, 4\}$  are defined as:

$$(M_1)_{ij}^{gh} = \delta_{ij} (1 - p^g) z^g \langle k^g \rangle f_i C^{gh} \frac{(1 - p^h) n_j^h}{(n_i^h)^{\text{eff}}}$$
(A5)

$$(M_2)_{ij}^{gh} = (1 - p^g) z^g \langle k^g \rangle f_i C^{gh} \frac{R_{ji}^h p^h n_j^h}{(n_i^h)^{\text{eff}}}$$
(A6)

$$(M_3)_{ij}^{gh} = p^g R_{ij}^g z^g \langle k^g \rangle f_j C^{gh} \frac{(1-p^h)n_j^h}{(n_j^h)^{\text{eff}}}$$
(A7)

$$(M_4)_{ij}^{gh} = \sum_{k=1}^{N} p^g R_{ik}^g z^g \langle k^g \rangle f_k C^{gh} \frac{R_{jk}^h p^h n_j^h}{(n_k^h)^{\text{eff}}}$$
(A8)

These tensors encode the four different ways in which the epidemic interactions may take place: individuals belonging to the same patch i = j and not moving  $(M_1)$ ; interaction in the patch of i with individuals coming from patch j  $(M_2)$ ; interaction in the patch of j with individuals coming from patch i  $(M_3)$ ; and individuals from i and j interacting at any other patch k  $(M_4)$ .

In the next generation matrix framework, we only need to consider the epidemic compartments. Making use of the above definitions, the corresponding differential equations take the form:

$$\dot{\rho}_i^{E,g} = -\eta^g \rho_i^{E,g} + \sum_{h=1}^{N_G} \sum_{j=1}^N M_{ij}^{gh} (b^A \rho_j^{A,h} + b^I \rho_j^{I,h})$$
(A9)

$$\dot{\rho}_i^{A,g} = \eta^g \rho_i^{E,g} - \alpha^g \rho_i^{A,g} \tag{A10}$$

$$\dot{\rho}_{i}^{I,g} = \alpha^{g} \rho_{i}^{A,g} - \mu^{g} \rho_{i}^{I,g} \tag{A11}$$

Where the tensor M is given by  $M = \sum_{\ell=1}^4 M_\ell$ . Defining the vector  $(\rho^g)^T = (\rho^{E,g}, \rho^{A,g}, \rho^{I,g})$ , the above system of differential equations can be rewritten as:

$$\dot{\rho}^g = \sum_{h=1}^{N_g} \left( F^{gh} - V^{gh} \right) \rho^h \tag{A12}$$

Where we defined  $V^{gh} = V^g \delta^{gh} \otimes \mathbb{1}_{N \times N}$  with:

$$V^g = \begin{pmatrix} \eta^g & 0 & 0 \\ -\eta^g & \alpha^g & 0 \\ 0 & -\alpha^g & \mu^g \end{pmatrix} \tag{A13}$$

And:

$$F^{gh} = \begin{pmatrix} \mathbb{O}_{N \times N} & b^A M^{gh} & b^I M^{gh} \\ \mathbb{O}_{N \times N} & \mathbb{O}_{N \times N} & \mathbb{O}_{N \times N} \\ \mathbb{O}_{N \times N} & \mathbb{O}_{N \times N} & \mathbb{O}_{N \times N} \end{pmatrix}$$
(A14)

With the above differential equation, the reproduction number is given by:

$$R_0 = \Lambda_{\text{max}}(FV^{-1}) \tag{A15}$$

We can calculate the inverse of the tensor V as  $(V^{-1})^{gh} = (V^g)^{-1}\delta^{gh} \otimes \mathbb{1}_{N\times N}$ . The inverse of the matrix  $V^g$  is given by:

$$(V^g)^{-1} = \begin{pmatrix} \frac{1}{\eta^g} & 0 & 0\\ \frac{1}{\alpha^g} & \frac{1}{\alpha^g} & 0\\ \frac{1}{\mu^g} & \frac{1}{\mu^g} & \frac{1}{\mu^g} \end{pmatrix}$$
(A16)

Accordingly, we have:

$$(FV^{-1})^{gh} = \begin{pmatrix} \left(\frac{b^A}{\alpha^g} + \frac{b^I}{\mu^g}\right) M^{gh} & \left(\frac{b^A}{\alpha^g} + \frac{b^I}{\mu^g}\right) M^{gh} & \frac{b^I}{\mu^g} M^{gh} \\ \mathbb{O}_{N \times N} & \mathbb{O}_{N \times N} & \mathbb{O}_{N \times N} \\ \mathbb{O}_{N \times N} & \mathbb{O}_{N \times N} & \mathbb{O}_{N \times N} \end{pmatrix}$$
(A17)

As we look for the eigenvectors of the tensor  $FV^{-1}$ , we note that their components associated to the compartments A and I—rows 2 and 3—must be zero, since the associated rows in the above matrix are zero. To be more precise, we have  $(FV^{-1}u)_i^g=0$  for  $i=2N+1,\ldots 3N$ , which are the elements associated to the compartments A and I. Accordingly, we can restrict the above matrix only to the vector space associated to the compartment E and the eigenvalues will be equivalent, which gives us:

$$R_0 = \Lambda_{\text{max}}(Z), \tag{A18}$$

where  $Z^{gh} = \left(\frac{b^A}{\alpha^h} + \frac{b^I}{\mu^h}\right) M^{gh}$ . Finally, the epidemic threshold is found by solving the implicit equation  $\Lambda_{\max}(Z) = 1$ .

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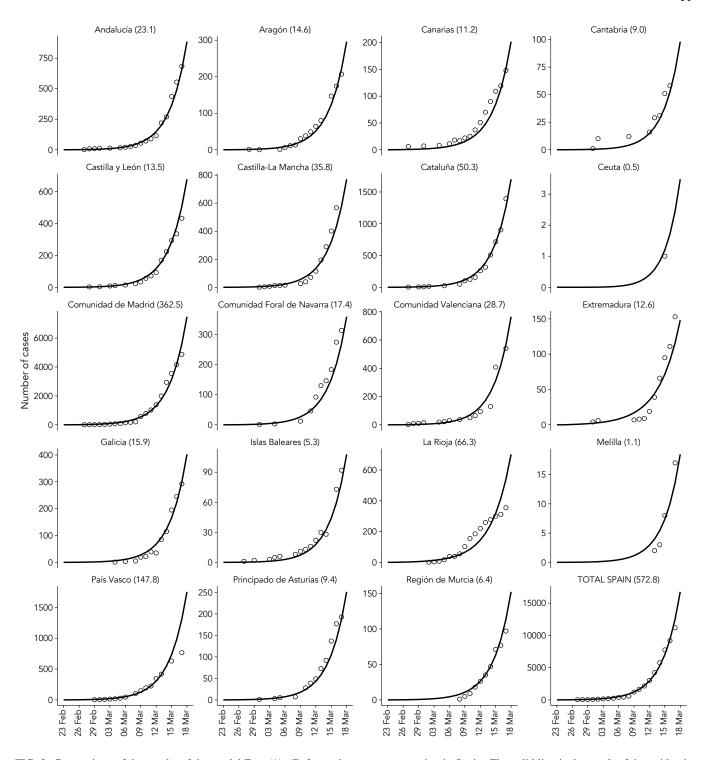


FIG. 2. Comparison of the results of the model Eqs. (1)–(7) for each autonomous region in Spain. The solid line is the result of the epidemic model, aggregated by ages, for the number of individuals inside compartments (H+R+D) that corresponds to the expected number of cases (see Figure 1), and dots correspond to real cases reported. The number appearing next to the region name corresponds to the Mean Absolute Error (MAE) between the model prediction and the total number of cases.

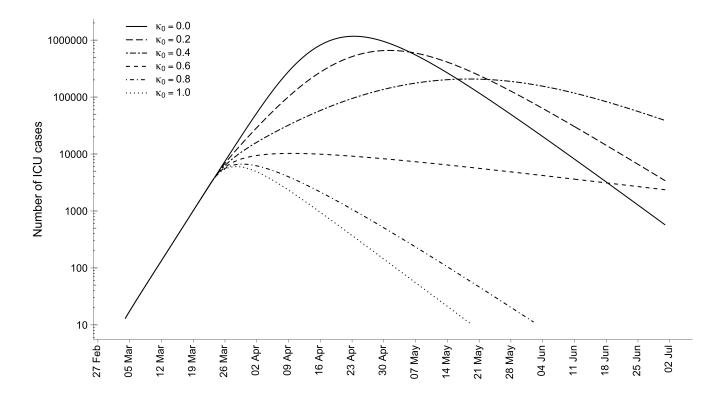


FIG. 3. Temporal evolution of the total number of ICU cases predicted for Spain as a function of the fraction of isolated population  $\kappa_0$  from March 20, 2020.

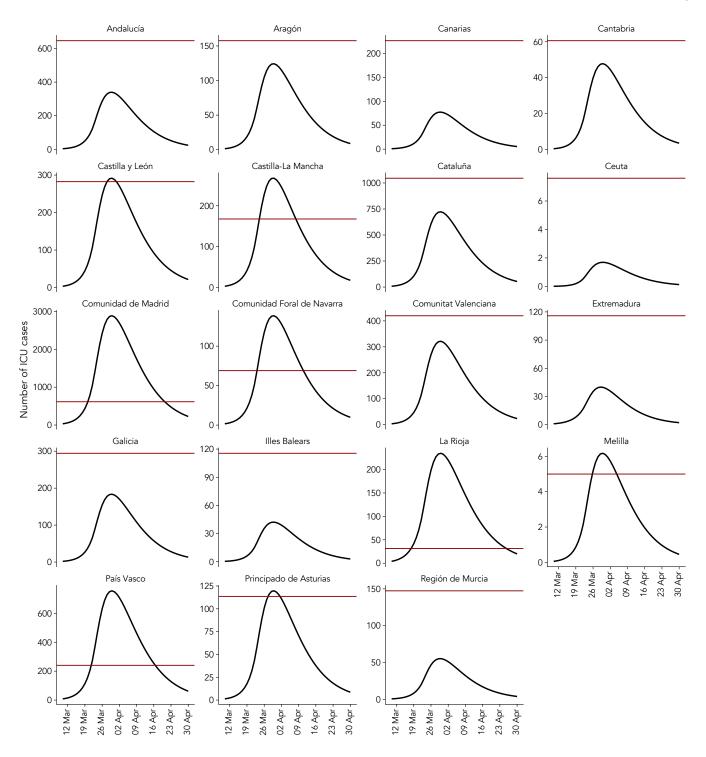


FIG. 4. ICU saturation curves for each region in Spain. The black lines shows the temporal evolution of individuals requiring ICU. The isolation of population is performed from March 20, 2020 with  $\kappa_0=0.80$ . The red line shows the estimated number of ICU beds for each autonomous region.